

Problem Set 3

1. *Medical.* Prices of medical services have been rising much faster than other goods and services in the economy. Let μ be medical services and x be all other goods. Suppose that a consumer has a demand curve for medical services of

$$\mu(p_\mu, p_x, m) = m - 30\sqrt{p_\mu} + 2p_x$$

- (a) In 2000, the prices were $p_x = 1$, $p_\mu = 1$, and $m = 40$. By 2007 prices had risen to $p'_x = 1.2$, $p'_\mu = 1.5$ and income had risen to $m' = 48$. Draw an indifference curve diagram, (with x on the x-axis) showing the two budget lines and the two optimal points. Remember that all income not spent on μ is spent on x .
- (b) Calculate the Laspeyres price index for the price change from 2000 to 2007.
- (c) Calculate the Paasche price index for the price change from 2000 to 2007.
- (d) If the consumer had been given a raise based on the Laspeyres price index, how much x and μ would she have consumed in 2007. Would her utility have been higher or lower than in 2000?
2. *Apartments.* Suppose the market demand curve for apartments is

$$x(p) = \left(100 - \frac{pm^2}{2880}\right)$$

x is the number of apartments rented, p is the monthly rent on a typical apartment, and m is the monthly income of a typical consumer in thousands of dollars.

- (a) If the current rent is \$900 and the current income is \$4, graph the demand curve and the Engel curve, labeling the current point and the intercepts.

- (b) Which of the following describe apartments at the current price and income: price elastic, price inelastic, necessity, luxury, normal, inferior. (Presumably people would rather own houses or condos if they have higher incomes.)
 - (c) If the price falls to \$800, what lump-sum tax or subsidy would leave the consumer able to purchase the same consumption bundle as before?
3. *Pate*. There are two goods, goose liver pate (G) and beef (B). The typical French person has an endowment of $\omega_G = 50, \omega_B = 50$ and a utility function $U(G, B) = G^{0.7} B^{0.3}$. The typical American has an endowment of $\omega_G = 30, \omega_B = 70$ and a utility function $U(G, B) = B^{0.8}$. Note that the typical American simply does not receive utility from the pate.
- (a) What is the typical French and American MRS in (B, G) space at the endowment points?
 - (b) Draw an Edgeworth box and show indifference curves for each type of consumer. Show the core and the contract curve.

Review Problems, not to turn in:

4. *Urp*. The residents of Uurp consume only pork chops (X) and Coca-Cola (Y). The utility function of the typical resident of Uurp is given by

$$U(X, Y) = \sqrt{XY}$$

In 2006, the price of pork chops in Uurp was \$1 each; Cokes were also \$1 each. The typical resident consumed 40 pork chops and 40 Cokes (saving is impossible in Uurp). In 2007, swine fever hit Uurp, and pork chop prices rose to \$4; the Coke price remained unchanged. At these new prices, the typical Uurp resident consumed 20 pork chops and 80 Cokes.

- (a) What was the change in utility from 2006 to 2007?
- (b) What was the Laspeyres price index for 2007?
- (c) What was the Paasche price index for 2007?

- (d) What do you conclude about the ability of price indices to measure changes in welfare? (Hint: calculate how much income the typical Urp resident had in 2006 and 2007.)

5. *AishaMrLee*. Aisha's utility function is

$$u(G, V) = G^{0.7}V^{0.3}$$

and Mr. Lee's utility function is

$$u(G, V) = G^{0.9}V^{0.1}$$

Aisha has 20 ounces of G and 10 ounces of V . Mr. Lee has 15 ounces of G and 15 ounces of V . This is all the G and V there is in the world, and there are no other people to trade with.

- (a) Calculate the MRS in (G, V) space for both consumers at the endowment point.
- (b) Draw an Edgeworth box showing the endowment and indifference curves of the consumers. (The indifference curves do not have to be plotted to match the utility function perfectly.)
- (c) Assume that Aisha and Mr. Lee can trade at a market price as price-takers. If we set G as the numeraire, what is the price of V ? What is the final allocation of G and V ?
- (d) Show the trading in your diagram.

Answers to Review Problems:

5. *Urp_a*.

(a)

$$\begin{aligned}U_{2006} &= \sqrt{40 \cdot 40} = 40 \\U_{2007} &= \sqrt{20 \cdot 80} = 40\end{aligned}$$

(b)

$$\frac{4 \cdot 40 + 1 \cdot 40}{1 \cdot 40 + 1 \cdot 40} = 2.5$$

(c)

$$\frac{4 \cdot 20 + 1 \cdot 80}{1 \cdot 20 + 1 \cdot 80} = 1.6$$

(d) We know that in actual fact, utility was unchanged and the new income in 2007 must have been $4 \cdot 20 + 1 \cdot 80 = 160$ which was twice the income of $1 \cdot 40 + 1 \cdot 40 = 80$ in 2000. Thus, Laspeyres overstated the amount of income needed to keep utility constant, and Paasche understated it.

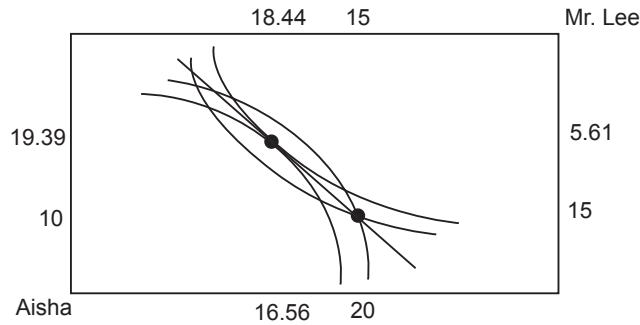
6. *AishaMrLee_a.*

(a)

$$MRS_A = -\frac{\frac{\partial u}{\partial G}}{\frac{\partial u}{\partial V}} = -\frac{.7G^{-.3}V^{.3}}{.3G^{.7}V^{-.7}} = -\frac{7V}{3G} = -\frac{7 \cdot 10}{3 \cdot 20} = -\frac{7}{6}$$

$$MRS_L = -\frac{\frac{\partial u}{\partial G}}{\frac{\partial u}{\partial V}} = -\frac{.9G^{-.1}V^{.1}}{.1G^{.9}V^{-.9}} = -9\frac{V}{G} = -9\frac{15}{15} = -9$$

(b) and (d)



(c) We have seen before that the demand functions for a Cobb-Douglas will produce the following results:

$$G_A = 0.7 \frac{m}{p_G} = 0.7 \frac{20 + 10p_V}{1}$$
$$G_L = 0.9 \frac{m}{p_G} = 0.9 \frac{15 + 15p_V}{1}$$

Thus, the market equilibrium condition is:

$$\begin{aligned}G_A + G_L &= 35 \\27.5 + 20.5p_V &= 35\end{aligned}$$

Solving this gives

$$20.5p_V = 7.5 \Rightarrow p_V = 0.366$$

This means that $G_A = 16.56$, $G_L = 18.44$, $V_A = 19.39$,
 $V_L = 5.61$.